Exercises April 26th 2004, Optimal Control of Economic Systems

1. Consider the system and cost criterion

$$\frac{d}{dt}x_1 = x_2 \quad x(0) = \begin{pmatrix} 1 & 0 \end{pmatrix}^T \qquad |u(t)| \le 1$$
$$\frac{d}{dt}x_2 = u \qquad \qquad J(u) = \int_0^4 (x_1(t) - x_2(t))dt$$

- (a) Determine the Hamiltonian and the equations for the co-state.
- (b) Determine the (candidate) optimal control and the corresponding state.
- 2. Exercise 2 of Section 4.5.
- 3. Exercise 4 of Section 4.5.