## Exercises April 26th 2004, Optimal Control of Economic Systems

1. Consider the system and cost criterion

$$
\begin{aligned}
& \frac{d}{d t} x_{1}=x_{2} \quad x(0)=\left(\begin{array}{ll}
1 & 0
\end{array}\right)^{T} \\
& \frac{d}{d t} x_{2}=u
\end{aligned}
$$

$$
\begin{array}{r}
|u(t)| \leq 1 \\
J(u)=\int_{0}^{4}\left(x_{1}(t)-x_{2}(t)\right) d t
\end{array}
$$

(a) Determine the Hamiltonian and the equations for the co-state.
(b) Determine the (candidate) optimal control and the corresponding state.
2. Exercise 2 of Section 4.5
3. Exercise 4 of Section 4.5

