

## Exercises werkcollege 6, FMSE

### Exercise 1

Consider the following FSP definitions:

$$\text{BUFFER} = (\text{in} \rightarrow \text{out} \rightarrow \text{BUFFER}).$$
$$|| \text{SYNC\_IN} = (\text{a}:\text{BUFFER} || \text{b}:\text{BUFFER}) / \{\text{in}/\{\text{a.in}, \text{b.in}\}\}.$$
$$|| \text{SYNC\_OUT} = (\text{c}:\text{BUFFER} || \text{d}:\text{BUFFER}) / \{\text{out}/\{\text{c.out}, \text{d.out}\}\}.$$
$$|| \text{SYSTEM} = ( \text{SYNC\_IN} / \{\text{sync.ac}/\text{a.out}, \text{sync.bd}/\text{b.out}\} \\ || \text{SYNC\_OUT} / \{\text{sync.ac}/\text{c.in}, \text{sync.bd}/\text{d.in}\} ) \\ @\{\text{in}, \text{out}\}.$$

- Give a structured graph of the labelled transition system of `SYSTEM`. Label the states with tuples  $(i, j, k, l)$ , where  $i, j, k, l$  are the respective local states of the processes  $\text{a}:\text{BUFFER}$ ,  $\text{b}:\text{BUFFER}$ ,  $\text{c}:\text{BUFFER}$  and  $\text{d}:\text{BUFFER}$ , who collectively determine the global state of `SYSTEM` (so you can't just copy the the LTSA output).
- Give a minimal automaton that is observation equivalent to `SYSTEM`. Give a sequential FSP process (i.e. without parallel composition or hiding) that is observation equivalent to `SYSTEM`.

### Exercise 2

Complete the MAZE example given in lecture 6 (slide 13). A path out of the maze is called *balanced* if and only if the number of north/south steps differs equals the number of east/west actions in the path. Modify your model such that for each initial square a shortest balanced path out of the maze, if it exists, is produced as a deadlock trace of the model. Determine the squares for which a balanced exit path exists.

### Exercise 3

One solution to the dining philosophers problem permits only 4 philosophers to sit down at the table at the same time. Specify a BUTLER process that, when composed with the model presented in lecture 6 (slide 9), permits a maximum of 4 philosophers to be seated concurrently at the table. Show that this system is deadlock-free.

### Exercise 4

What action trace violates the following safety property?

$$\text{property PS} = (\text{a} \rightarrow (\text{b} \rightarrow \text{PS} | \text{a} \rightarrow \text{PS}) | \text{b} \rightarrow \text{a} \rightarrow \text{PS}).$$

### **Exercise 5**

A lift has a maximum capacity of ten people. In the model of the lift control system, passengers entering a lift are signalled by an `enter` action and passengers leaving the lift are signalled by an `exit` action. Specify a safety property in FSP that when composed with the lift will check that the system never allows the lift to have more than 10 occupants.